

```
In [1]: # define y=f(x)
#
f(x)=sqrt(x+1)
show(f)
```

Out[1]: $x \mapsto \sqrt{x+1}$

```
In [2]: # finding dydx
#
dydx=diff(f(x),x)
show(dydx)
```

Out[2]:
$$\frac{1}{2\sqrt{x+1}}$$

```
In [3]: # finding ds
#
ds=sqrt(1+(dydx)^2).simplify_rational()
show(ds)
```

Out[3]:
$$\frac{1}{2} \sqrt{\frac{4x+5}{x+1}}$$

```
In [4]: # 2*pi*y*ds
show(2*pi*f(x)*ds.canonicalize_radical())
```

Out[4]:
$$\pi\sqrt{4x+5}$$

```
In [5]: # the area of surface of rotation about x-axis
#
show(integrate(2*pi*f(x)*ds.canonicalize_radical(),x,0,1,hold=true))
```

Out[5]:
$$\int_0^1 \pi\sqrt{4x+5} dx$$

```
In [6]: show(integrate(2*pi*f(x)*ds.canonicalize_radical(),x,0,1))
```

Out[6]:
$$-\frac{1}{6} \pi(5\sqrt{5} - 27)$$

```
In [7]: RR(integrate(2*pi*f(x)*ds.canonicalize_radical(),x,0,1))
```

Out[7]: 8.28315466528680

```
In [8]: # the area of surface of rotation about y-axis
#
show(integrate(2*pi*x*ds.canonicalize_radical(),x,0,1,hold=true))
```

Out[8]:

$$\int_0^1 \frac{\pi\sqrt{4x+5x}}{\sqrt{x+1}} dx$$

```
In [9]: show(integrate(2*pi*x*ds.canonicalize_radical(),x,0,1))
```

Out[9]:

$$\frac{1}{64} \pi (28\sqrt{5} + 12\sqrt{2} + 17 \log(4\sqrt{5} + 9) - 17 \log(12\sqrt{2} + 17))$$

```
In [10]: RR(integrate(2*pi*x*ds.canonicalize_radical(),x,0,1))
```

Out[10]: 3.37380879355257

In [0]: