

## The Hong Kong Polytechnic University Department of Applied Mathematics

# Colloquium

On

### **Proximal Methods for Sparsity-reducing Regularization**

by

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#### Abstract

We consider the minimization of the sum of two convex functions in the case where one of them is convex and differentiable, and the other is convex and non-differentiable. The latter plays the role of reducing sparsity. A typical example is the minimization problem

$$\min_{x} \frac{1}{2} \|\Phi x - u\|_{2}^{2} + \gamma \|x\|_{1}, \qquad (*)$$

where  $\Phi$  is an  $m \times n$  matrix and  $u \in \mathbb{R}^m$  is given. Since the  $\ell$  1-norm is viewed as a sparsity-reducing norm, the problem (\*) is used to approximate the nonconvex sparse optimization problem

$$\min_{x \to 0} \|x\|_0 \quad \text{subject to} \quad \|\Phi x - u\|_2 \le \varepsilon. \tag{(**)}$$

Here  $||x||_0$  is the  $\ell$  0-norm of  $\square\square$ (i.e., the number of nonzero components of  $\square$ ).

In this talk, I will discuss the proximal methods for minimizing the sum of two convex functions in general, and the minimization problem (\*) in particular.

| Date  | : | May 4, 2012 (Friday)                        |
|-------|---|---|
| Time  | : | 2:00 p.m. – 3:00 p.m.                       |
| Venue | : | DE408, The Hong Kong Polytechnic University |

\*\*\* ALL ARE WIELCOME \*\*\*