



**The Hong Kong Polytechnic University  
Department of Applied Mathematics**

**Seminar**

On

**Estimation of Pure Characteristics Demand Models  
with Pricing**

by

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**Abstract**

A pure characteristics model (PCM) is a class of discrete-choice random-coefficients demand models in which there is no idiosyncratic logit error term in a consumer's utility. The absence of the logit error term leads to a nonsmooth formulation of the predicted market share equations. As a result, inverting the market share equations for the unobserved product characteristics and estimating the model by using the nested fixed-point approach becomes computationally intractable. We introduce lotteries for consumers' purchase decisions, which are then characterized by a system of complementarity constraints. This reformulation leads to smooth market share equations. As a result, we can reformulate the generalized method of moments (GMM) estimation of a pure characteristics model as a quadratic program with nonlinear complementarity constraints. The reformulation of consumers' decision problem provides a unified framework to study the Nash-Bertrand pricing problem under pure characteristics demand models and the GMM estimation of the demand model with pricing equations. We present numerical results to demonstrate the effectiveness of our approach.

**Date : July 16, 2012 (Monday)**

**Time : 2:30 p.m. – 3:30 p.m.**

**Venue : HJ610, The Hong Kong Polytechnic University**

**\* \* \* ALL ARE WELCOME \* \* \***